Algebra III/Trig			
Unit	Priority Standards	Supporting Standards	AMPLICA TO AN EL 🛥
	CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.	CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.	
1 - Functions		CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.	
		CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.	
er:	22.	CC.2.2.HS.C.6 Interpret functions in terms of the situations they model.	-
	CC.2.2.HS.D.6 Extend the knowledge of rational	CC.2.1.HS.F.1 Apply and extend the properties of exponents to	A Lieb
	functions to rewrite in equivalent forms.	solve problems with rational exponents. CC.2.2.HS.D.2 Write expressions in equivalent forms to solve	•
		problems.	
		CC.2.2.HS.D.3 Extend the knowledge of arithmetic operations and apply to polynomials.	
2 - Rationals		CC.2.2.HS.D.4 Understand the relationship between zeros and factors of polynomials to make generalizations about functions and their graphs.	
		CC.2.2.HS.D.5 Use polynomial identities to solve problems.	
		CC.2.2.HS.D.7 Create and graph equations and inequalities to describe numbers or relationships.	
		CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable.	
			the subject of the second seco
	CC.2.2.HS.C.5 Construct and compare linear, quadratic, and exponential models to solve	CC.2.1.HS.F.1 Apply and extend the properties of exponents to solve problems with rational exponents.	
	problems.	CC.2.2.HS.D.7 Create and graph equations and inequalities to describe numbers or relationships.	
		CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable.	
3 - Exponentials &		CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.	
Logarithms		CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.	
		CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.	
		CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.	
		CC.2.2.HS,C.6 Interpret functions in terms of the situations they model.	
di .	CC.2.2.HS.C.7 Apply radian measure of an angle	CC.2.1.HS.F.2 Apply properties of rational and irrational numbers	
	and the unit circle to analyze the trigonometric functions.	to solve real world or mathematical problems.	
4 - Trigonometric	CC.2.2.HS.C.8 Choose trigonometric functions to model periodic phenomena and describe the properties of the graphs.	CC.2.1.HS.F.4 Use units as a way to understand problems and to guide the solution of multi-step problems.	
		CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems.	
			4
4 - Trigonometric Functions		CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context.	
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		CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.	
		CC.2.2.HS.C.6 Interpret functions in terms of the situations they model.	
		CC.2.3.HS.A.7 Apply trigonometric ratios to solve problems involving right triangles.	
5 - Trigonometric	CC.2.2.HS.C.7 Apply radian measure of an angle and the unit circle to analyze the trigonometric functions.	CC.2.2.HS,D.1 Interpret the structure of expressions to represent a quantity in terms of its context.	
	CC.2.2.HS.C.8 Choose trigonometric functions to model periodic phenomena and describe the properties of the graphs.	CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems.	
Identities & Applications	CC.2.2.HS.C.9 Prove the Pythagorean identity and use it to calculate trigonometric ratios.	CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable.	
		CC.2.2.HS.D.9 Use reasoning to solve equations and justify the solution method.	
		CC.2.2.HS.D.10 Represent, solve, and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically.	

CV Priority Standard/PA Core Standard

CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions.

Taught in Unit(s)

Unit 1 - Functions

Explanation/Example of Standard

Analyze graphs and their translations on the coordinate plane. Identify domain, range & other properties of functions & their graphs.

Common Misconceptions

Students switch the domain and range of the function.

When evaluating composition of functions, students will multiply instead of substituting one function's range into another's domain.

When solving for an inverse function, students will improperly apply the order of operations.

When shifting graphs, students will move the opposite direction.

Big Idea(s)

Mathematical functions are relationships that assign each member of one set (domain) to a unique member of another set (range), and the relationship is recognizable across representations.

Families of functions exhibit properties and behaviors that can be recognized across representations. Functions can be transformed, combined, and composed to create new functions in mathematical and real world situations.

Essential Question(s)

How do you explain the benefits of multiple methods of representing polynomial functions (tables, graphs, equations, and contextual situations)?

How do quadratic equations and their graphs and/or tables help us interpret events that occur in the world around us?

How are relationships represented mathematically?

How can data be organized and represented to provide insight into the relationship between quantities?

Assessments

See unit map for specific unit common assessments.

Concepts

(what students need to know)

Function vs. Relations

Function notation

Domain and Range

Transformations of functions

Inverses

Vertical line test

Relative maximum and minimum

Piecewise functions

Compositions of functions

Even vs. Odd Functions

Skills

(what students must be able to do)

Identify relations that are functions.

Evaluate functions.

Identify domain and range of functions.

Identify increasing and decreasing intervals.

Determine relative maximums and minimums.

Graph piecewise functions.

Apply rigid and nonrigid transformations to

graphs.

Determine and evaluate composition of functions.

Determine the inverse of a function.

CV Priority Standard/PA Core Standard

CC.2.2.HS.D.6 Extend the knowledge of rational functions to rewrite in equivalent forms.

Taught in Unit(s)

Unit 3 - Rationals

Explanation/Example of Standard

Simplify rational expressions. Solve rational equations. Graph rational functions.

Common Misconceptions

When students simplify a rational expression, they will cancel individual terms instead of entire factors. When adding and subtracting rational expressions, students will simplify without finding a common denominator.

Students will not factor a rational expression before simplifying.

Students think that rational expression rules are different when variables are involved.

Students switch horizontal and vertical asymptotes and x & y intercepts.

Big Idea(s)

Mathematical relationships can be represented as expressions, equations, and inequalities in mathematical situations.

Numerical quantities, calculations, and measurements can be estimated or analyzed by using appropriate strategies and tools.

Patterns exhibit relationships that can be extended, described, and generalized.

Essential Question(s)

How are relationships represented mathematically?

How is mathematics used to quantify, compare, represent, and model numbers?

How is mathematics used to quantify, compare,

represent, and model numbers? How can expressions, equations, and inequalities be used to quantify, solve, model, and/or analyze

mathematical situations?

Assessments

See unit map for specific unit common assessments.

Concents

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: 	(what students need to know)
	Rules of Exponents
	Properties of Radicals
	Operations with Polynomials (binomial,
	trinomial, etc.)
	Operations with Rational Expressions
	Complex Fractions
	Graphs of Rational Functions
	Vertical & Horizontal Asymptotes
	Domain of Rational Functions

Range of Rational Functions

Skills

(what students must be able to do) Simplify rational expressions.

Simplify radical expressions.

Rationalize numerators and denominators.

Perform operations with polynomials.

Factor polynomials.

Identify domain of algebraic expressions.

Analyze graphs of rational functions

Sketch graphs of rational functions.

CV Priority Standard/PA Core Standard

CC.2.2.HS.C.5 Construct and compare linear, quadratic, and exponential models to solve problems.

Taught in Unit(s)

Unit 2 - Exponential and Logarithmic Functions

Explanation/Example of Standard

Solve exponential and logarithmic equations.

Analyze exponential and logarithmic graphs.

Solve real - world problems using exponential and logarithmic models.

Common Misconceptions

Students wrongly manipulate exponential and logarithmic equations.

Students misunderstand the domains of exponential and logarithmic graphs.

Students misuse logarithmic properties when simplifying logarithmic expressions.

Students forget to check for extraneous solutions when solving logarithmic equations.

Big Idea(s)

Numbers, measures, expressions, equations, and inequalities can represent mathematical situations and structures in many equivalent forms.

Patterns exhibit relationships that can be extended, described, and generalized.

- Relations and functions are mathematical relationships that can be represented and analyzed using words, tables, graphs, and equations.
- There are some mathematical relationships that are always true and these relationships are used as the rules of arithmetic and algebra and are useful for writing equivalent forms of expressions and solving equations and inequalities.
- Mathematical functions are relationships that assign each member of one set (domain) to a unique member of another set (range), and the relationship is recognizable across representations.
- Families of functions exhibit properties and behaviors that can be recognized across representations. Functions can be transformed, combined, and composed to create new functions in mathematical and real world situations.
- Mathematical relationships among numbers can be represented, compared, and communicated.
- Mathematical relationships can be represented as expressions, equations, and inequalities in mathematical situations.
- Patterns exhibit relationships that can be extended, described, and generalized.
- Mathematical relations and functions can be modeled through multiple representations and analyzed to raise and answer questions.

Essential Question(s)

How can you extend algebraic properties and processes to quadratic, exponential and polynomial expressions and equations and then apply them to solve real world problems? What are the advantages/disadvantages of the various methods to represent exponential functions (table, graph, equation) and how do we choose the most appropriate representation? How can expressions, equations, and inequalities be used to quantify, solve, model, and/or analyze mathematical situations?

How are relationships represented mathematically?

How is mathematics used to quantify, compare, represent, and model numbers?
How can patterns be used to describe relationships in mathematical situations?

Assessments

See unit map for specific unit common assessments.

Concepts	Skills
(what students need to know)	(what students must be able to do)
Exponential Function	Evaluate exponential and logarithmic functions.
Natural Exponential Function	Solve exponential and logarithmic equations.
Logarithmic Function	Condense and expand logarithmic expressions.
Common Logarithmic Function	Model and solve real - life applications using
Natural Logarithmic Function	exponential and logarithmic functions.
Properties of Logarithms	
Exponential & Logarithmic Equations	
Exponential & Logarithmic Models	
Exponential growth and decay functions	

CV Priority Standard/PA Core Standard

CC.2.2.HS.C.7 Apply radian measure of an angle and the unit circle to analyze the trigonometric functions.

Taught in Unit(s)

Unit 4 - Trigonometric Functions

Explanation/Example of Standard

Determine exact values of all six trigonometric ratios for the special angles.

Know all 16 special angles (in radians and degrees) and the coordinates of each on the unit circle.

Common Misconceptions

Students will switch sine and cosine and how they relate to the coordinates.

Students will multiply by the wrong ratio when converting from radians to degrees and vice versa. Students will not pay attention to the quadrant in which the angle lies.

Big Idea(s)

Numbers, measures, expressions, equations, and inequalities can represent mathematical situations and structures in many equivalent forms.

Some geometric relationships can be described and explored as functional relationships.

Relations and functions are mathematical relationships that can be represented and analyzed using words, tables, graphs, and equations.

Patterns exhibit relationships that can be extended, described, and generalized.

Essential Question(s)

How can you use coordinates and algebraic techniques to represent, interpret, and verify trigonometric relationships? How can patterns be used to describe relationships in mathematical situations? How can recognizing repetition or regularity assist in solving problems more efficiently?

How can trigonometric properties and theorems be used to describe, model, and analyze situations?

Assessments

See unit map for specific unit common assessments.

Concepts

(what students need to know)

Trigonometry Sine, Cosine, Tangent

Cosecant, Secant, Cotangent

Initial Side

Terminal Side

Standard Position

Coterminal Angle

Reference Angle

Radian Angle

Degree Angle

Positive and Negative Angle

Unit Circle

Skills

(what students must be able to do)

Identify all six trigonometric functions of an

Convert between radians and degrees.

Identify the reference angle and any coterminal

angle for the given angle..

Draw an angle in standard position.

CV Priority Standard/PA Core Standard

CC.2.2.HS.C.8 Choose trigonometric functions to model periodic phenomena and describe the properties of the graphs.

Taught in Unit(s)

Unit 4 - Trigonometric Functions, Unit 5 - Trigonometric Identities and Applications

Explanation/Example of Standard

Graph sine and cosine functions.

Identify the parameters of the graphs.

Common Misconceptions

Students misunderstand the graphs of sine and cosine and where they begin.

Students confuse the period with the angular frequency.

When determining the translations from a trigonometric equation, students switch the direction of the translations.

When dealing with inverse sine and cosine, students confuse the domain restriction that allow for an inverse function.

Big Idea(s)

Numbers, measures, expressions, equations, and inequalities can represent mathematical situations and structures in many equivalent forms.

Some trigonometric relationships can be described and explored as functional relationships.

Relations and functions are mathematical relationships that can be represented and analyzed using words, tables, graphs, and equations.

Graphs can be transformed in an infinite number of ways. Transformations can be described and analyzed mathematically.

Essential Question(s)

How can you use coordinates and algebraic techniques to represent, interpret, and verify trigonometric relationships?
How can patterns be used to describe relationships in mathematical situations?
How can recognizing repetition or regularity assist in solving problems more efficiently?
How can trigonometric properties and theorems be used to describe, model, and analyze situations?

Assessments

See unit map for specific unit common assessments.

Concepts	Skills
(what students need to know)	(what students must be able to do)
Amplitude	Identify amplitude, period, phase shift and
Period	vertical shift of a trigonometric equation and
Translations	graph.
Transformations	Sketch translations of sine and cosine graphs.
Inverse Sine	Model real - life data using sine and cosine
Inverse Cosine	functions.
Angular Frequency	Solve trigonometric equations using inverse sine
	and cosine.

CV Priority Standard/PA Core Standard

CC.2.2.HS.C.9 Prove the Pythagorean identity and use it to calculate trigonometric ratios.

Taught in Unit(s)

Unit 4 - Trigonometric Functions, Unit 5 - Trigonometric Identities and Applications

Explanation/Example of Standard

Using the pythagorean identity to find trigonometric values.

Verify trigonometric identities.

Finding the values of the six trigonometric functions using right triangles.

Common Misconceptions

When verifying identities, students will manipulate both sides of the equation.

Students find incorrect ratios of sine, cosine and tangent.

Students make fundamental algebra mistakes when using the pythagorean identity to find trigonometric values.

Students confuse cosecant and secant and which one is the reciprocal function for sine and cosine.

Big Idea(s)	Essential Question(s)
Numbers, measures, expressions, equations, and inequalities can represent mathematical situations and structures in many equivalent forms. Mathematical statements can be justified through deductive and inductive reasoning and proof.	How do you use the ideas of direct and indirect proof, and counter-examples to verify valid conjectures and refute invalid conjectures? How can you use coordinates and algebraic techniques to represent, interpret, and verify trigonometric relationships? How can patterns be used to describe relationships in mathematical situations? How can trigonometric properties and theorems be used to describe, model, and analyze situations?

Assessments

See unit map for specific unit common assessments.

Concepts	Skills
(what students need to know)	(what students must be able to do)
Sine, Cosine, Tangent	Evaluate trigonometric functions using
Reciprocal Identities	trigonometric identities or right triangles.
Cosecant, Secant, Cotangent	Verify trigonometric identities.
Pythagorean Identities	Simplify trigonometric expressions.
Quotient Identities	
Right Triangle Trigonometry	
Sum and Difference Angle Identities	